

## Implementation of high-resolution time-to-digital converter in 8-bit microcontrollers

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This paper will demonstrate how a time-to-digital converter (TDC) with sub-nanosecond resolution can be implemented into an 8-bit microcontroller using so called “direct” methods. This means that a TDC is created using only five bidirectional digital input–output-pins of a microcontroller and a few passive components (two resistors, a capacitor, and a diode). We will demonstrate how a TDC for the range 1–10  $\mu\text{s}$  is implemented with 0.17 ns resolution. This work will also show how to linearize the output by combining look-up tables and interpolation. © 2012 American Institute of Physics. [<http://dx.doi.org/10.1063/1.3700192>]

### I. INTRODUCTION

A time-to-digital converter (TDC) quantizes the time between a start and a stop signal and they are either analog or counter-based.<sup>1–3</sup> Analog TDCs use the start and stop signals to generate a pulse with a length corresponding to the start and stop times, this pulse is then converted into an analog voltage by an integrator, and then an analog-to-digital converter (ADC) digitizes this voltage, see Figure 1.

The aim of this work was to design a high-resolution (sub-nano) TDC using a simple inexpensive 8-bit microcontroller only. For several reasons, the analog TDC technique in Figure 1 was discarded. First, the ADC in popular microcontrollers such as Microchip’s PIC18 family of controllers has a resolution of only 10 bits.<sup>4</sup> Second, we would like our design to work also for inherently digital systems like field programmable gate arrays (FPGAs) and complex programmable logic devices.

Hence, we need to focus on counter-based TDCs. A “basic” counter-based TDC simply counts the pulses from a reference clock during the start and stop interval, see Figure 2.

Since the start and stop signals are asynchronous with the reference clock, there will be an inherent  $\pm 1$  count uncertainty, and hence the time resolution is limited by the reference clock’s speed.<sup>1</sup> However, increasing the clock frequency raises two issues; first the power consumption increases and second there is a limit to the maximum oscillator frequency that can be implemented in CMOS.<sup>1</sup> (If the start and stop signals are asynchronous to the reference clock, the resolution can be increased by averaging.)

An 8-bit PIC-controller from Microchip running with a 20 MHz crystal will internally run at 5 MHz.<sup>4</sup> Using its embedded 16-bit timers for time interval measurements, using the basic counting technique, would render a maximum time resolution of  $\pm 200$  ns. In order to achieve sub-nano resolution (without averaging) we need more advanced methods.

There are a few commonly used principles that can be implemented in order to increase the resolution of counter-based TDCs; tapped delay-lines, vernier clocks, or time stretching. Tapped delay-lines use digital buffers as delay elements where each buffer’s output is connected to the input of an edge-

triggered flip-flop. The flip-flops are latched by the stop signal arriving some time later, producing a “temperature”-coded time interval value on the flip-flops’ output,<sup>1,5</sup> see Figure 3.

This is a very fast, high-resolution TDC and sometimes is referred to as a “flash TDC” (representing the TDC correspondence to flash ADCs<sup>6,7</sup>). Even though the tapped delay-line solution is fast and all-digital, it is not suitable for implementation in “fixed-hardware” targets such as microcontrollers; there are simply no buffers and flip-flops available on-chip.

In the vernier principle, high-resolution TDCs are implemented by employing two oscillators with slightly different frequencies  $f_1 = 1/T_1$  and  $f_2 = 1/T_2$ , respectively.<sup>1,2,8,9</sup> The start and stop signals trigger one oscillator each, see Figure 4.

Oscillator 1, with frequency  $f_1 (<f_2)$ , starts on the positive edge of the start signal. The second oscillator, with frequency  $f_2$ , is triggered on the positive edge of the stop signal. Since  $f_2 > f_1$ , the pulses from the  $f_2$ -oscillator will eventually catch up with the pulses from the  $f_1$ -oscillator. When this happens, both counters are stopped (and notice that at this point both oscillators have generated exactly the same number of pulse, i.e.,  $N_1 = N_2 = N$ ). From Figure 4 it is obvious that

$$\tau = N_1 T_1 - N_2 T_2 = N (T_1 - T_2) = N \times \Delta T. \quad (1)$$

The time resolution depends on the time difference  $\Delta T$  of the clocks’ cycle periods. This idea could be implemented in a microcontroller as long as it has two separate timers/counters that can be clocked independently. However, it would be hard to reach the theoretical time resolution  $\Delta T$  if we implemented this method in a typical microcontroller from Atmel/Microchip/Freescale. In order to achieve the theoretical time resolution  $\Delta T$ , we would have to be able to compare the timer registers in hardware; comparing timer registers in a polling firmware algorithm is too time consuming and we

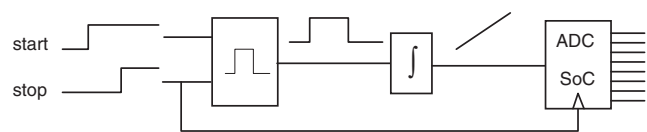


FIG. 1. Schematic principle of analog TDC.

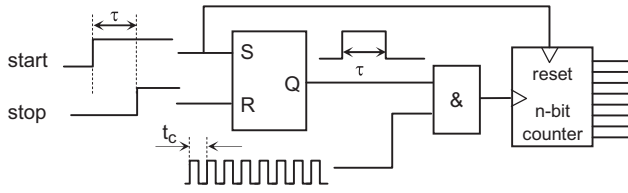


FIG. 2. Schematic principle of basic counting TDC.

would most likely miss the moment of timers' coincidence. That method was indeed examined in this work and when we used an 8-bit PIC18F controller from Microchip, the minimum uncertainty in the moment of coincidence detection was  $\pm 30$  counts (for  $\Delta T = 4.6$  ns). Neither Microchip nor Atmel has any 8-bit controllers that can compare two 16-bit timer registers in hardware. (They can compare 16-bit registers in hardware, just not two running timer registers in real-time.)

In order to implement a high-resolution TDC in an 8-bit controller, we are left with the technique of time stretching. In the basic counter-based TDC, the time resolution is  $\pm t_c$ ,  $t_c$  being the oscillator clock cycle period in Figure 2; if we count  $N$  pulses, our estimate of the time interval  $\tau$  is

$$\hat{\tau} = (N \pm 1) \times t_c. \quad (2)$$

The resolution is  $t_c$  and the uncertainty is  $\pm t_c$ . Suppose we stretch the time interval by a factor of  $k$ , see Figure 5.

If we measure the stretched time interval  $\tau'$  with the same instrument as in Figure 2, we would get  $N'$  pulses:

$$\hat{\tau}' = (N' \pm 1) \times t_c = N' t_c \pm t_c, \quad (3)$$

but since  $\tau = \tau'/k$ , our estimate of  $\tau$  is

$$\hat{\tau} = \frac{1}{k} \hat{\tau}' = N' \frac{t_c}{k} \pm \frac{t_c}{k}. \quad (4)$$

Hence, if the time is stretched by a factor of  $k$ , both the resolution and the uncertainty are improved by a factor of  $k$ .

There are several ways to stretch a time interval and Figure 6 illustrates the basic principle; charging and discharging of a capacitor.<sup>10,11</sup>

In Figure 6 it is assumed that  $i_1 \gg i_2$ . The capacitor is charged during  $\tau$  by a constant current  $i_1 - i_2$  and then discharged by  $i_2$  only. This will produce a prolonged pulse on the comparator's output that will be  $k = i_1/i_2$  times longer than  $\tau$ .<sup>10</sup>

This paper will describe how time stretching can be implemented with a simple 8-bit microcontroller and a few pas-

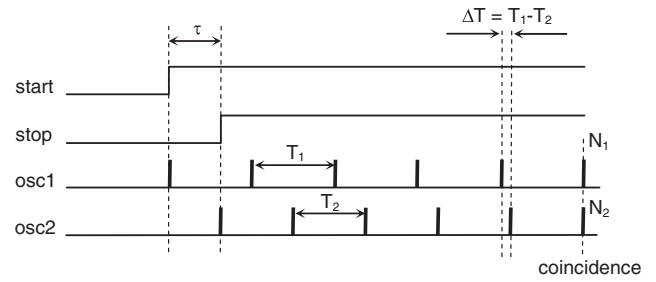


FIG. 4. The vernier principle.

sive components only. The rest of this paper is organized as follows; in Sec. II we will present a new time stretching idea that can be implemented in a microcontroller with only a few passive external components. This idea is based on the “direct sensor-to-controller”<sup>12-18</sup> and “direct analog-to-controller”<sup>19</sup> techniques and therefore these techniques are introduced first. In Sec. III we analyze the proposed circuit and present some theoretical expressions and design rules. In Sec. IV we present some experimental results and in Sec. V we briefly describe how a look-up table (LUT) is implemented in order to produce a linear output response. Section VI summarizes the reported work and results and draws some final conclusions.

## II. THE “DIRECT” MICROCONTROLLER TECHNIQUE

In the late 1990s, several reports were published concerning the technique of “direct” interfacing of passive sensors to microcontrollers.<sup>12,13</sup> With this technique, passive sensors such as resistive thermal devices (RTDs) and capacitive humidity sensors can be interfaced to digital embedded systems that do not have an embedded ADC. Figure 7 illustrates the fundamental idea.

The technique is based on the fact that digital input-output (I/O)-pins on a typical microcontroller (or FPGA) are bidirectional and reconfigurable in firmware; as inputs they represent high-impedance (high-Z) loads and as outputs they represent low-impedance loads that can be either sourcing (set high) or sinking (set low). In Figure 7,  $R_S$  represents the RTD and  $R_C$  represents a calibration resistor. During the first stage, I/O-pins 1 and 2 are configured as inputs (high-Z) and I/O-pin 3 is configured as output and set high. I/O-pin 3 will charge the capacitor to  $V_{OH}$  (=the output high voltage of I/O-pin 3). During the second stage, the capacitor is discharged through  $R_S$  by reconfiguring I/O-pin 2 to out-

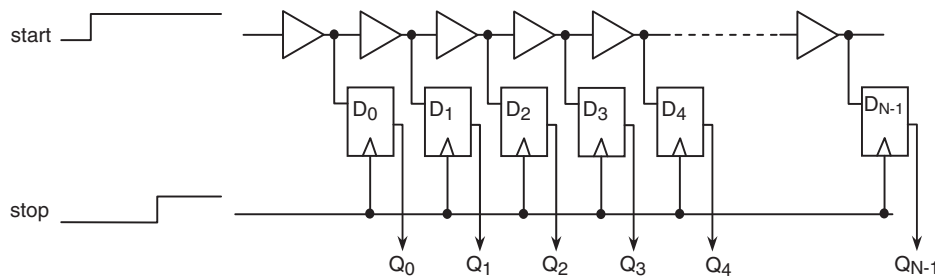


FIG. 3. A basic delay-line for generation of clock cycle subdivisions.



FIG. 5. Time stretching.

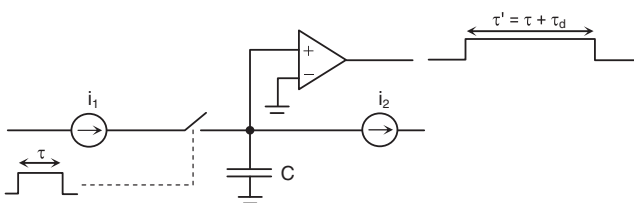
put (set low) and I/O-pin 3 is reconfigured to input. I/O-pin 3 is polled in firmware until the capacitor has been discharged to  $V_{IL}$  (=input logic low threshold of I/O-pin 3). An internal timer measures this time (producing an integer  $N_S$ ). Next, the charging/discharging procedure is repeated, but now the capacitor is discharged through  $R_C$ , and the internal timer produces an integer  $N_C$ . From these two integers, the unknown resistance  $R_S$  may be estimated:<sup>12</sup>

$$\hat{R}_S = \frac{N_S}{N_C} \times R_C. \quad (5)$$

Richey<sup>20</sup> suggested a similar method for direct interfacing of capacitive sensors and Reverter and Casas<sup>21</sup> presented a similar solution for differential capacitive sensors. In 2001, Custodio *et al.*<sup>14</sup> presented a direct approach to the interfacing of bridge sensors and in 2012, Bengtsson<sup>19</sup> reported a work on how to interface analog voltage output sensors “directly” to digital embedded systems.

This work now suggests a “direct” microcontroller solution for TDC implementation by time stretching. The idea is illustrated in Figure 8.

At first, all I/O-pins are configured as inputs (high-Z), except for I/O-pin 4 that is configured as output and set low. When the controller is interrupted (on the interrupt pin) by the positive pulse edge, the capacitor is charged via  $R_1$  during the time interval  $\tau$ ;  $C$  will be charged to a voltage proportional to the time interval  $\tau$ . I/O-pin 1 is polled in order to detect the negative edge (=the stop signal). When I/O-pin 1 senses the negative pulse edge, I/O-pin 2 is reconfigured to output and set low and the capacitor is discharged through  $R_2$ . (Notice how the diode directs all discharging current into  $R_2$ .) At the same time as I/O-pin 1 detects the negative pulse edge, I/O-pin 4 is also set high. Assuming that the capacitor was charged to a voltage  $>V_{IH}$  (input voltage logic high for I/O-pin 3), polling I/O-pin 3 will detect the time it takes for the capacitor to discharge to  $V_{IL}$  (input voltage logic low for I/O-pin 3). When  $V_{IL}$  is detected, I/O-pin 4 is reset. The pulse width of I/O-pin 4 will be a stretched version of the input pulse if  $R_2 \gg R_1$ ; Figure 8 is indeed a pulse stretcher and may be used for implementing high resolution TDCs in 8-bit microcontrollers (and of course 16/32-bit controllers too). Figure 9 illustrates the firmware flowchart.

FIG. 6. Time stretching by Nutt.<sup>10</sup>

### III. SYSTEM ANALYSIS

Figure 10 illustrates the equivalent circuit during the charging.

If  $U_{in}$  is the amplitude of the input pulse and  $U_d$  is the voltage drop across the diode, the capacitor  $C$  is charged by a voltage  $U_0 = U_{in} - U_d$  during the time interval  $\tau$ . After time  $\tau$ ,  $C$  is charged to  $U_\tau$ :

$$U_\tau = U_0 \times (1 - e^{-\tau/R_1 C}). \quad (6)$$

For this design to work, it is important that the time constant  $R_1 C$  is chosen such that  $U_\tau > V_{IH}$ ;  $U_\tau$  must be large enough so that it exceeds the input logic high threshold of I/O-pin 3. This will set a limit to the minimum pulse width we can analyze. On the other hand, the capacitor should not be saturated ( $U_\tau < U_0$ ) because if it is saturated,  $\tau$  cannot be uniquely determined. For the design to work reliably, we require that the capacitor is never charged to more than  $\sim 99\%$  of  $U_0$ . That gives us the following conditions:

$$V_{IH} < U_\tau < 0.99U_0. \quad (7)$$

Inserting (6) into (7) gives us

$$V_{IH} < U_0 \times (1 - e^{-\tau/R_1 C}) < 0.99U_0 \quad (8)$$

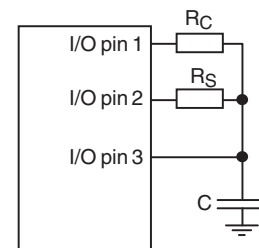
and from Eq. (8) we get either a condition for  $R_1 C$  depending on the desired range of  $\tau$  or an expected range of  $\tau$  for any given time constant  $R_1 C$ :

$$-R_1 C \times \ln \left\{ 1 - \frac{V_{IH}}{U_0} \right\} < \tau < 4.606 \times R_1 C, \quad (9)$$

$$-\frac{\tau}{\ln \left\{ 1 - \frac{V_{IH}}{U_0} \right\}} < R_1 C < 0.2171 \times \tau, \quad (10)$$

where  $\tau$  must be in the range given by Eq. (9) for  $C$  to be charged to a voltage in the recommended range  $V_{IH}$ – $0.99U_0$ .

During phase 2, the capacitor is discharged through  $R_2$ . The equivalent circuit is illustrated in Figure 11.

FIG. 7. The one-point calibration “direct” technique.<sup>12</sup>

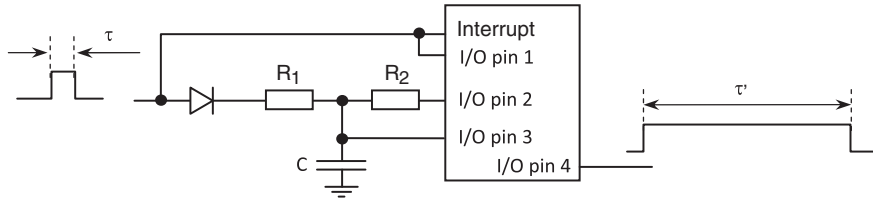


FIG. 8. A “direct” microcontroller TDC.

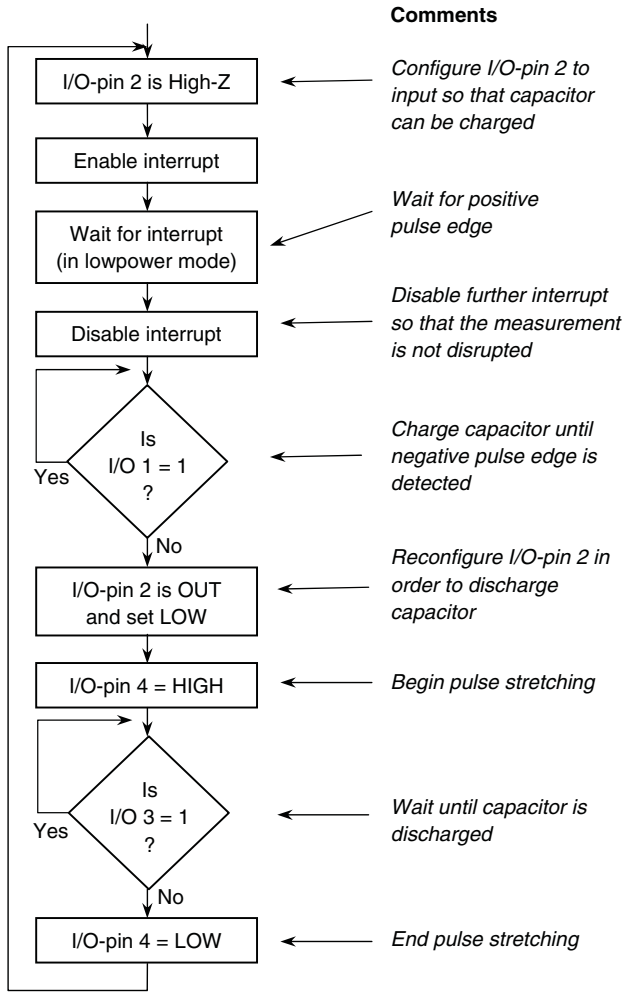


FIG. 9. Firmware flowchart.

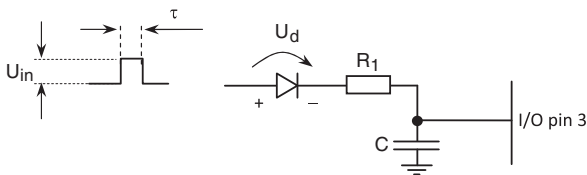


FIG. 10. Equivalent system circuit during charging.

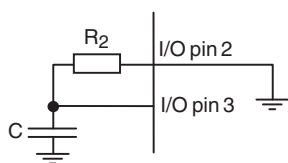


FIG. 11. Equivalent circuit during discharging.

If the capacitor voltage  $U_\tau > V_{IH}$  at  $\tau = 0$ , it will take some time  $t_d$  to discharge it to  $V_{IL}$ :

$$U_d(t) = U_\tau \times e^{-t/R_2C} \Rightarrow t_d = -R_2C \times \ln \left\{ \frac{V_{IL}}{U_\tau} \right\}, \quad (11)$$

$$t_d = -R_2C \times \ln \left\{ \frac{V_{IL}}{U_0(1 - e^{-\tau/R_1C})} \right\},$$

where  $t_d$  is the time during which I/O-pin 4 is set high. Dividing by the input pulse width gives us the time expansion factor  $k$ :

$$k = \frac{t_d}{\tau} = \frac{\tau'}{\tau} = -\frac{R_2C}{\tau} \times \ln \left\{ \frac{V_{IL}}{U_0(1 - e^{-\tau/R_1C})} \right\}. \quad (12)$$

**IV. EXPERIMENTAL RESULTS**

The time stretching technique in Figure 8 was implemented in a PIC18F4580 microcontroller from Microchip.<sup>4</sup> The  $V_{IL}$  and  $V_{IH}$  parameters were measured, as described by Reverter *et al.*,<sup>18</sup> to 1.23825 V and 1.25384 V, respectively. To generate the input pulse, we used a HP8013B pulse generator and  $U_0$  was measured to 3.16 V using a Tektronix oscilloscope TDS2012B. In order to demonstrate the idea and to verify theoretical expressions, we first chose the time constants to get a range of approximately 10–100  $\mu$ s.  $R_1$  and  $R_2$  were measured to 99.71  $\Omega$  and 8.078 k $\Omega$ , respectively (using a Phillips PM2534 DMM and the 4-wire method).  $C$  was measured to 207 nF (measured with a HP4216A LCR meter). According to expression (9), this suggests a range for  $\tau$  as follows:

$$10.43 \times 10^{-6} \text{s} < \tau < 95.05 \times 10^{-6} \text{s}.$$

In Figure 12 we have plotted experimentally registered data; measured stretch factor versus input pulse width. For comparison we have also plotted expression (12) in the same diagram.

As we can see in Figure 12, observed data deviates some from the theoretical predictions. The theoretical predictions represent expression (12) and we examined that for some small disturbances in  $C$  and  $U_0$ , and it turns out to be very sensitive to these variations. A possible explanation for the deviations between observed data and theoretical predictions is first that the total capacitance is not just the capacitor  $C$ ; the equivalent circuit diagram should probably also include the diode’s capacitance. The diode capacitance is particularly important at high frequencies and when the diode operates in the reverse direction<sup>22,23</sup> (as it does during discharging). Another contribution to the deviations from the theoretical prediction is that the diode distorted the input pulse shape, so that it was

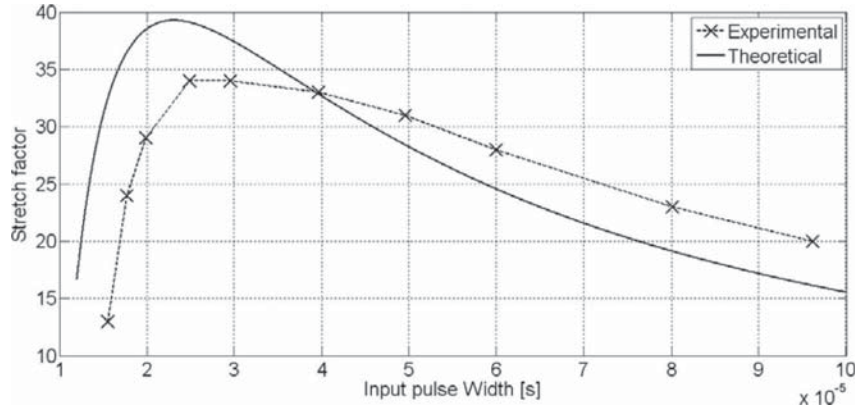


FIG. 12. Observed stretch factor compared with theoretical stretch factor.

not a perfect square. We have not further investigated the exact details behind the deviations; the observed data follows the predictions to a satisfactory degree. The relationship is non-linear (as expected) and that means that it has to be linearized by implementing a LUT. The fact that it does not exactly follow the theoretical prediction is not crucial since it has to be calibrated with a LUT anyway.

Next we decided to stress the design by designing a TDC for some smaller range. The internal timer of the microcontroller can be clocked at 5 MHz at most (if the external crystal is 20 MHz), corresponding to a clock cycle period of 200 ns. That means that a time interval of 1  $\mu$ s would only yield a few counts and a  $\pm 20\%$  uncertainty. Time stretching (or some other vernier method) will be necessary to get a “decent” resolution/uncertainty. Suppose we want to detect time intervals in the range 1–10  $\mu$ s, with a precision of 0.1%. That would require a resolution of 1 ns for the “low” interval end and 10 ns for the “high” interval end. If we stretch the interval by a factor of 1000, a 10  $\mu$ s pulse would be stretched to 10 ms. The maximum range of a 16-bit timer clocked at a rate of 5 MHz is 13.1 ms ( $2^{16} \times 200$  ns), so that would be within our boundaries. Using design equation (10), we chose  $R_1 = 90.68 \Omega$  (measured),  $C = 23.2$  nF (measured) and, using expression (11), we chose  $R_2 = 470.9$  k $\Omega$  (measured). Figure 13 illustrates the calibration results of this time stretching design.

In the plot in Figure 13 we have also fitted data to the non-linear expression (12) (using the *nlfit()* command in MATLAB). We can rewrite expression (12) in the following way:

$$\begin{aligned} k = f(\tau) &= \frac{t_d}{\tau} = \frac{\tau'}{\tau} = -\frac{R_2 C}{\tau} \times \ln \left\{ \frac{V_{IL}}{U_0(1 - e^{-\tau/R_1 C})} \right\} \\ &= \frac{R_2 C}{\tau} \times \left\{ \ln(1 - e^{-\tau/R_1 C}) - \ln \frac{V_{IL}}{U_0} \right\} \\ &= \frac{a}{\tau} \times \{ \ln((1 - e^{-\tau/b}) + c) \}, \end{aligned} \quad (13)$$

where parameters  $a = R_2 C$ ,  $b = R_1 C$ , and  $c = -\ln(V_{IL}/U_0)$ . The experimental data in Figure 13 was fitted to a function described by expression (13) and this fitted curve is the continuous line in the plot in Figure 13.

## V. IMPLEMENTING LUT IN AN 8-BIT MICROCONTROLLER

If we multiply expression (13) by  $\tau$ , we get an expression for the stretched time  $\tau'$  that we measure. If we measure this time  $\tau'$  using an on-chip (16-bit) timer it will produce an

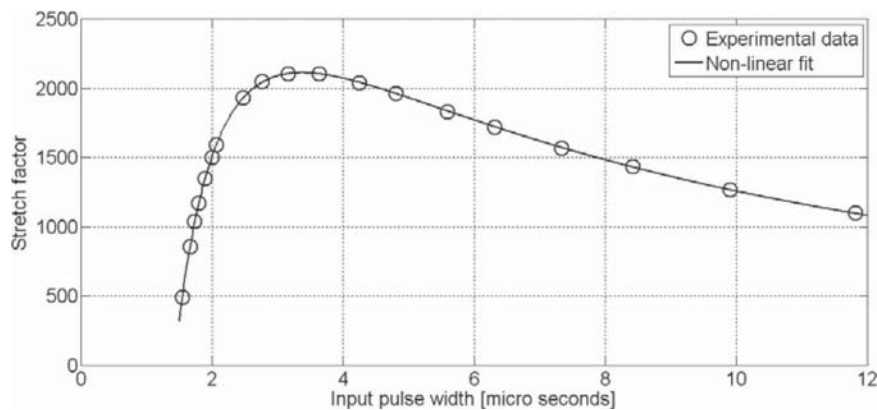


FIG. 13. Stretch factor versus pulse width.

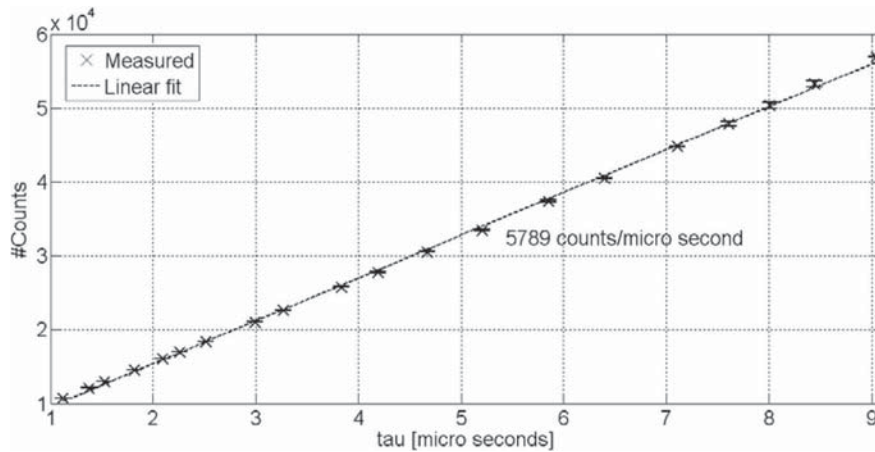


FIG. 14. TDC output count versus input time interval.

integer  $N$ . If the timer is clocked with a cycle period of  $t_c$ , then  $\tau' = N \times t_c$ :

$$\tau' = N \times t_c = a \times \{\ln(1 - e^{-\tau/b}) + c\}. \quad (14)$$

Parameters  $a$ ,  $b$ , and  $c$  are known from the curve fitting in Figure 13. Solving for  $\tau$  in Eq. (14) gives us

$$\tau = -b \times \ln(1 - e^{N \times t_c / a - c}). \quad (15)$$

We could use expression (15) to implement a LUT consisting of  $2^{16}$  double-typed fractional  $\tau$ -values. However, this would be a very memory-intensive solution and as we are implementing our solution in an embedded system, we are looking for a less memory-demanding solution. First, we want to work with integers instead of double-typed fractional (since a 16-bit integer only needs half the memory space of a double fractional). From Figure 13 we can see that the useful  $\tau$ -range in the real experiment was  $12 \mu\text{s}$  (measured to 12.4). Hence, if we multiply all  $\tau$ -values in expression (15) by  $2^{16}/12.4 = 5285$ , and round to nearest integer, we convert all  $\tau$ -values into an integer range that fits into a 16-bit counter's range.

Second, we only generate the  $\tau$ -values in (15) for 256 (equidistant)  $N$ -values, and our LUT will consist of these 256  $\tau$ -values only (multiplied by 5285); we use linear interpolation to find intermediate values. Notice how well this works out in an 8-bit firmware algorithm; we can use the eight most significant bits of the 16-bit timer as a pointer for the LUT and we use the eight least significant bits for the linear interpolation. In an 8-bit microcontroller they are already available in separate registers anyway. Notice that the overall linearity of the design will depend only on the accuracy of the LUT entries, the sparseness of the LUT, the resolution of the (piecewise) linear interpolation, and the curviness of the function in expression (15).<sup>25,26</sup>

In Figure 14 we present the output of our TDC after having implemented a linearizing LUT as described above. The looked-up counter value was transferred to a host Windows computer via an asynchronous serial interface.

The error bars in Figure 14 represent one standard deviation and varied from 10 to 400 counts due to stochastic variations in  $\tau$ . (Notice that a small uncertainty  $\Delta\tau$  in  $\tau$  propagates into an uncertainty  $k \times \Delta\tau$  in the stretched time inter-

val.) The 5789 counts/ $\mu\text{s}$  indicates a potential time resolution of 0.17 ns.

## VI. CONCLUSIONS

There are many situations in science and engineering that require accurate and high-resolution time measurements. This includes propagation delay measurements on integrated circuits, time domain reflectometry in cables (TDR), radar ranging, nuclear, and ballistic time of flight measurements. Also, since time can be measured more cost-efficient<sup>24</sup> than voltage, a lot of sensors produce pulse width modulated signals that need accurate, high-resolution time measurements.

This work has demonstrated how a sub-nano resolution TDC can be implemented in an 8-bit microcontroller with "direct" methods. We have demonstrated how pulse widths in the range 1–10  $\mu\text{s}$  can be stretched by a factor of 1000–2000 times. Measuring this stretched time using a microcontroller embedded counter clocked at 200 ns yields a sub-nano resolution. The method is general and can easily be adjusted for other time intervals, however there are some limitations. First, the *minimum time interval* range that can be detected is determined by the  $R_1C$  time constant,  $V_{IH}$ , and  $U_0$ ; during time  $\tau$ , the capacitor  $C$  must be charged to a voltage exceeding  $V_{IH}$ . This indicates that we should choose  $R_1C$  as small as possible in order to make sure it is charged to the proper voltage level during  $\tau$ . However, the *maximum time interval* is also determined by  $R_1C$ ; all time intervals that saturate  $C$  (charge  $C$  to  $U_0$ ) will produce the same stretched time  $\tau'$  and we would not be able to uniquely resolve them.

It was observed that for repetitive measurements the produced integer varied. This is due to stochastic variations in  $\tau$  and can be reduced by averaging. The overall conversion speed of the proposed TDC corresponds basically to the stretched time. In our design example the maximum stretched time was 12.4 ms and the worst-case conversion time was less than 13 ms. Notice that this conversion time is not affected by the fact that we transfer data to a host computer via an asynchronous serial link; the data transfer of the last sample takes place during the discharging time of the next sample, so no time is lost.

The proposed design in Figure 8 requires 5 digital I/O-pins. Of course, I/O-pin 4 is not really necessary if an internal timer is used to measure the stretched time. Also, the proposed design measures the *pulse width*. Some additional circuitry is needed in order to measure the time interval between two separate start and stop signals; a simple SR latch will do if the start signal is connected to the “Set” input and the stop signal is connected to the “Reset” input, the SR latch’s Q output will generate a pulse that can be inserted into our TDC design in Figure 8. This is illustrated in Figure 2.

From expression (12) we can see that the stretch factor  $k$  depends on the passive components ( $R_1$ ,  $R_2$ , and  $C$ ) and on the  $U_0$  and  $V_{IL}$  parameters. All the passive components are known to have temperature dependence and  $U_0$  depends on the diode’s voltage drop in forward biased mode which is also known to depend on temperature. (The temperature dependence of  $V_{IL}$  is not known.) Because of the temperature dependence of the parameters in expression (12) the stretch factor  $k$  most certainly suffers from temperature variations but that has not been examined further in this work.

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